

NUMERICAL PREDICTION OF THE MEAN WIND  
OVER WATER WAVES

Kenneth G. Dunning

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# NAVAL POSTGRADUATE SCHOOL

## Monterey, California



# THESIS

NUMERICAL PREDICTION OF THE MEAN WIND  
OVER WATER WAVES

by

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Thesis Advisor:

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March 1974

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Numerical Prediction of the Mean Wind  
Over Water Waves

by

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## ABSTRACT

Stauffer (1973) developed a theoretical model for the prediction of air flow above ocean waves. In this study his results were extended with the addition of buoyance effects and two different lower boundary conditions.

Through numerical solutions it was possible to determine that:

1) mean wind velocities at lower levels closely approximate the initial mean velocity profile for large wave numbers ( $k \geq 0.45\text{m}^{-1}$ ) or small wave amplitudes, 2) mean wind velocities at lower levels fluctuate more from the initial mean velocity profile as the wave number decreased or the wave amplitude increases, 3) solutions were very sensitive to the level where the velocity gradient is computed in the lower boundary condition, 4) disturbance potential temperature at lower levels increases inversely with wave number, and 5) the presence of temperature fluctuations has an insignificant effect on the Reynolds stress or on the stream function. The numerical solutions show general agreement with the observational analyses of wave modified wind profiles by Davidson (1974). However, these comparisons are not conclusive because of the sensitivity in the lower boundary condition.





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TABLE OF SYMBOLS AND ABBREVIATIONS

A	-	stream function amplitude (cosine coefficient)
a	-	wave amplitude
B	-	stream function amplitude (sine coefficient)
c	-	phase speed
$c_p$	-	specific heat at constant pressure
D	-	potential temperature amplitude (cosine coefficient)
E	-	potential temperature amplitude (sine coefficient)
G	-	acceleration of gravity
H	-	height of the boundary layer
K	-	coefficient of turbulent exchange of momentum which is related to the mean velocity gradient
$K_\theta$	-	coefficient of turbulent exchange of heat which is related to the mean velocity gradient
k	-	wave number
$\kappa$	-	von-Karman's constant ( $\kappa = 0.35$ )
$\lambda$	-	wavelength
$\nu$	-	coefficient of turbulent exchange of momentum associated with the wave-caused velocity fluctuations
$\nu_m$	-	coefficient of molecular viscosity
$\nu_\theta$	-	coefficient of turbulent exchange of heat associated with the wave-caused velocity fluctuations
P	-	pressure
$R_m$	-	steady state condition
t	-	time
$T_*$	-	temperature scale



$\tau$  - Reynolds stress ( $m^2/sec^2$ )  
 $\theta$  - potential temperature fluctuation  
 $\theta$  - disturbance potential temperature  
 $\theta_o$  - domain mean potential temperature ( $\theta_o = 300^\circ K$ )  
 $U$  - mean horizontal velocity  
 $u$  - total velocity in x-direction  
 $u'$  - turbulent velocity fluctuation  
 $U_*$  - dynamic velocity  
 $W$  - total wind velocity  
 $w$  - vertical velocity  
 $\psi$  - stream function  
 $\psi_o$  - stationary portion of the stream function  
 $z$  - height  
 $z_1$  - false lower level  
 $z_o$  - roughness parameter  
 $\xi$  - vorticity ( $\nabla^2\psi$ )



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## I. INTRODUCTION

The forerunner of this study (Stauffer, 1973) used a theoretical numerical model to investigate wave-related momentum transfer. The model was used to obtain the Reynolds wave stress of the perturbation-velocity field in the atmospheric layer above ocean waves. The study was similar to that of Yefimov (1970) and utilized an initial value numerical procedure similar to that of Newman (1969). Equations were solved by utilizing central differencing in general but with the turbulence terms evaluated at the previous time step. Solution separation was avoided by incorporating the Matsuno (1966) finite difference scheme every 50 time steps. Experiments were run varying the independent variables: wave number ( $k$ ), dynamic velocity ( $U_*$ ), roughness parameter ( $z_0$ ), and the coefficient of turbulent exchange ( $\nu$ ). The measure of the error in the change of the stress in air ( $R$ ) was computed at each time step and calculations continued until the stress reached a steady state condition defined by  $R \leq 1 \times 10^{-5}$ . Maximum Reynolds stress occurred at about one meter above the wave surface, and the largest momentum transfer was found to exist for the largest mean wind speeds, lowest wave numbers, and a turbulent coefficient of approximately  $0.02 \text{ m}^2/\text{sec}$ . The magnitude of the Reynolds stress increased as the





mean wind velocity approached that of the wave phase speed in the lowest levels of the boundary layer. Thus when the wave velocity is close to the mean wind velocity in the lower levels, the disturbance energy is the greatest.

The emphasis in this study is on the changes in the mean wind which are caused by the wave stresses which were computed by Stauffer (1973). His basic model is modified to include buoyancy effects which arise during non-neutral conditions. Also the lower boundary condition was changed to include the mean wind shear. Two approximations to this boundary condition were investigated. Experiments were carried out in which the following quantities were varied: wave number ( $k$ ), grid size, convergence criteria, wave amplitude ( $a$ ), and lower boundary condition. It was found that the mean wind departed from the logarithmic profile in the lower region when the wave number became small and when the wave amplitude was large. Some of these variations were consistent with the observations of Davidson (1974).



## II. DEVELOPMENT OF THE MODEL

Development of the model is similar to that of Stauffer (1973). The Boussinesq equations for two dimensional motion take the following form:

$$\frac{\partial W}{\partial t} + W \cdot \nabla W = - \nabla \pi - \frac{g \Theta}{\Theta_0} k + F, \quad (2.1)$$

$$\frac{\partial \Theta}{\partial t} + W \cdot \nabla \Theta = - \frac{\partial}{\partial x} (\overline{u' \theta'}) - \frac{\partial}{\partial z} (\overline{w' \theta'}) , \text{ and} \quad (2.2)$$

$$\frac{\partial u}{\partial x} + \frac{\partial w}{\partial z} = 0 , \quad (2.3)$$

where

$$F_x = \frac{\partial}{\partial x} (\overline{-u'^2}) + \frac{\partial}{\partial z} (\overline{-u' w'}) ,$$

$$F_z = \frac{\partial}{\partial x} (\overline{-u' w'}) + \frac{\partial}{\partial z} (\overline{-w'^2}) ,$$

$$\pi = c_p \Theta_0 (p_0/p)^K + gz ,$$

$$\Theta = T(p_0/p)^K - \Theta_0 , \quad \text{and}$$

$$K = R/c_p .$$

Here  $T(p_0/p)^K$  is the total potential temperature,  $\Theta_0$  is the mean potential temperature for the whole region,  $R$  is the universal gas constant,  $c_p$  is the specific heat at constant pressure,  $x$  is the horizontal axis, and  $z$  is the vertical axis. Equation (2.1) is the equation of motion; equation (2.2) is the first law of thermodynamics, and equation (2.3) is the continuity equation. The



quantities  $u'$ ,  $w'$ , and  $\theta'$  are turbulent fluctuations. A straight line above a variable signifies the stationary part (time averaged) of each variable, and a wavy line represents the non-stationary part (space averaged). The velocity ( $W$ ) and the potential temperature ( $\Theta$ ) are broken up as follows:

$$W = (U(x,t) + u(x,z,t)) \mathbf{i} + w \mathbf{k} , \text{ and} \quad (2.4)$$

$$\Theta = \bar{\Theta}(z,t) + \theta(x,z,t) . \quad (2.5)$$

Following Yefimov (1970), the turbulent fluxes are approximated as follows:

$$-\overline{u'w'} = \tau = K \frac{\partial U}{\partial z} + v \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right) , \quad (2.6)$$

$$\overline{u'^2} = \overline{w'^2} , \quad (2.7)$$

$$-\overline{w'\theta'} = K_\theta \frac{\partial \Theta}{\partial z} + v_\theta \frac{\partial \theta}{\partial z} , \text{ and} \quad (2.8)$$

$$-\overline{u'\theta'} = v_\theta \frac{\partial \theta}{\partial x} . \quad (2.9)$$

Here  $K$  and  $K_\theta$  are the coefficients of turbulent exchange for the mean fields, and  $v$  and  $v_\theta$  are the coefficients of the wave-caused fluctuations.

The following vorticity equation is formed by taking  $\mathbf{j} \cdot \nabla \mathbf{x}$  with equation (2.1):

$$\begin{aligned} \frac{\partial \xi}{\partial t} + U \frac{\partial \xi}{\partial x} + w \frac{\partial^2 U}{\partial z^2} + u \frac{\partial \xi}{\partial x} + w \frac{\partial \xi}{\partial z} = \\ \frac{\partial^2}{\partial z^2} \left[ K \frac{\partial u}{\partial z} + v \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right) \right] - v \left( \frac{\partial^3 u}{\partial x^2 \partial z} + \frac{\partial^3 w}{\partial x^3} \right) - \frac{g}{\Theta_0} \frac{\partial \theta}{\partial x} , \end{aligned} \quad (2.10)$$



where

$$\xi = \frac{\partial u}{\partial z} - \frac{\partial w}{\partial x} . \quad (2.11)$$

In this derivation, equations (2.3), (2.4), (2.5), (2.6), and (2.7) have been used. When equations (2.4), (2.5), (2.8), and (2.9) are introduced into equation (2.2) it becomes:

$$\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + w \frac{\partial \tilde{\theta}}{\partial z} + u \frac{\partial \theta}{\partial x} + w \frac{\partial \theta}{\partial z} = \frac{\partial}{\partial z} (K_{\theta} \frac{\partial \tilde{\theta}}{\partial z}) + v_{\theta} \left( \frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial z^2} \right) . \quad (2.12)$$

These derivations have used the following assumptions:

$$\frac{\partial \tilde{\theta}}{\partial t} \approx 0 , \quad \frac{\partial u}{\partial t} \approx 0 \quad (2.13)$$

Take the x-average of equations (2.10) and (2.12):

$$u \frac{\partial \xi}{\partial x} + w \frac{\partial \xi}{\partial z} = \frac{\partial^2}{\partial z^2} (K \frac{\partial u}{\partial z}) , \quad (2.14)$$

$$u \frac{\partial \theta}{\partial x} + w \frac{\partial \theta}{\partial z} = \frac{\partial}{\partial z} (K_{\theta} \frac{\partial \tilde{\theta}}{\partial z}) . \quad (2.15)$$

Subtract (2.14) and (2.15) from (2.10) and (2.12), respectively, and neglecting products of the fluctuation quantities gives:

$$\frac{\partial \xi}{\partial t} + u \frac{\partial \xi}{\partial x} + w \frac{\partial^2 u}{\partial z^2} = \frac{\partial^2}{\partial z^2} [v \left( \frac{\partial u}{\partial z} + \frac{\partial w}{\partial x} \right)] - v \left[ \frac{\partial^3 u}{\partial x^2 \partial z} + \frac{\partial^3 w}{\partial x^3} \right] - \frac{g}{\theta_0} \frac{\partial \theta}{\partial x} , \quad (2.16)$$

$$\frac{\partial \theta}{\partial t} + u \frac{\partial \theta}{\partial x} + w \frac{\partial \tilde{\theta}}{\partial z} = v_{\theta} \left[ \frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial z^2} \right] . \quad (2.17)$$





Since the motion is non-divergent (equation (2.3)), a stream function can be defined such that:

$$u = \frac{\partial \psi}{\partial z}, \quad w = -\frac{\partial \psi}{\partial x}. \quad (2.18)$$

When these relations are introduced into (2.16) and (2.17), they become:

$$\begin{aligned} \frac{\partial}{\partial t} \left[ \frac{\partial^2 \psi}{\partial z^2} + \frac{\partial^2 \psi}{\partial x^2} \right] = & -U \left[ \frac{\partial^3 \psi}{\partial x \partial z^2} + \frac{\partial^3 \psi}{\partial x^3} \right] + \frac{\partial \psi}{\partial x} \frac{\partial^2 U}{\partial z^2} \\ & + \frac{\partial^2}{\partial z^2} \left[ v \left( \frac{\partial^2 \psi}{\partial z^2} - \frac{\partial^2 \psi}{\partial x^2} \right) \right] - v \left[ \frac{\partial^4 \psi}{\partial x^2 \partial z^2} - \frac{\partial^4 \psi}{\partial x^4} \right] - \frac{g}{\theta_0} \frac{\partial \theta}{\partial x} \end{aligned} \quad (2.19)$$

$$\frac{\partial \theta}{\partial t} = -U \frac{\partial \theta}{\partial x} + \frac{\partial \psi}{\partial x} \frac{\partial \theta}{\partial z} + v_{\theta} \left[ \frac{\partial^2 \theta}{\partial x^2} + \frac{\partial^2 \theta}{\partial z^2} \right]. \quad (2.20)$$

In this study the motions are forced by a surface wave of wave number ( $k$ ) and phase speed ( $c$ ). Therefore, the stream function and the potential temperature departure are written as:

$$\psi = A(z, t) \cos [k(x-ct)] + B(z, t) \sin [k(x-ct)], \quad (2.21)$$

$$\theta = D(z, t) \cos [k(x-ct)] + E(z, t) \sin [k(x-ct)]. \quad (2.22)$$

Substitute relations (2.21) and (2.22) into (2.19) and separate the cosine and sine terms. Equating the coefficients of the cosine terms gives:

$$\begin{aligned} \frac{\partial}{\partial t} \left[ \frac{\partial^2 A}{\partial z^2} - k^2 A \right] = & k(U-c) \left( Bk^2 - \frac{\partial^2 B}{\partial z^2} \right) + Bk \frac{\partial^2 U}{\partial z^2} \\ & + \frac{\partial^2}{\partial z^2} \left[ v \left( \frac{\partial^2 A}{\partial z^2} + Ak^2 \right) \right] + vk^2 \left[ \frac{\partial^2 A}{\partial z^2} + Ak^2 \right] - \frac{gkE}{\theta_0} \end{aligned} \quad (2.23)$$



The coefficients of the sine terms give:

$$\begin{aligned} \frac{\partial}{\partial t} \left[ \frac{\partial^2 B}{\partial z^2} - k^2 B \right] &= -k(U-c) \left( Ak^2 - \frac{\partial^2 A}{\partial z^2} \right) - Ak \frac{\partial^2 U}{\partial z^2} \\ &+ \frac{\partial^2}{\partial z^2} \left[ v \left( \frac{\partial^2 B}{\partial z^2} + Bk^2 \right) \right] + vk^2 \left[ \frac{\partial^2 B}{\partial z^2} + Bk^2 \right] + \frac{gkD}{\theta_o} \end{aligned} \quad (2.24)$$

If the same procedure is carried out with equation (2.20), the cosine coefficients give:

$$\frac{\partial D}{\partial t} = -k(U-c)E + \frac{\partial \tilde{\theta}}{\partial z} kB - v_{\theta} \left[ Dk^2 - \frac{\partial^2 D}{\partial z^2} \right] \quad (2.25)$$

The sine terms give:

$$\frac{\partial E}{\partial t} = -k(c-U)D + \frac{\partial \tilde{\theta}}{\partial z} kA - v_{\theta} \left[ Ek^2 - \frac{\partial^2 E}{\partial z^2} \right] \quad (2.26)$$

Substitute (2.21) into (2.14) yields:

$$\frac{k}{2} \frac{\partial}{\partial z} \left[ A \frac{\partial^2 B}{\partial z^2} - B \frac{\partial^2 A}{\partial z^2} \right] = \frac{\partial^2}{\partial z^2} \left( k \frac{\partial U}{\partial z} \right) \quad (2.27)$$

Equation (2.15) will not be used in this study because it turns out that the temperature effects are very small.

Therefore  $\tilde{\theta}$  is equal to its initial value in this study.

The equations (2.23) through (2.27) form a complete set in the variables A, B, D, E, and U.



### III. BOUNDARY CONDITIONS AND INITIAL CONDITIONS

Yefimov (1970) defined the boundary conditions for the lower boundary of the turbulent layer as:

$$U(\eta, t) + (x, \eta, t) = -akc \cos [k(x-ct)] , \quad (3-1)$$

$$w(x, \eta, t) = akc \sin [k(x-ct)] , \quad (3-2)$$

where the height of the wave surface is given by:

$$\eta = a \cos [k(x-ct)] . \quad (3.3)$$

The deep water wave phase speed is:  $c = (g/k)^{1/2}$  . (3.4)

If (3.1) and (3.2) are in terms of the stream function (2.18), they can be written as:

$$U(\eta, t) + \frac{\partial \psi}{\partial z} (x, \eta, t) = akc \cos [k(x-ct)] , \quad (3.5)$$

$$- \frac{\partial \psi}{\partial x} (x, \eta, t) = akc \sin [k(x-ct)] . \quad (3.6)$$

The stream function and its derivatives at  $z = \eta$  can be approximated by the values at  $z = 0$ , but  $U(\eta, t)$  cannot be approximated by  $U(0, t)$  since  $U$  has a very rapid change near the surface. Therefore  $U(\eta, t)$  is expressed with a Taylor series expansion as:

$$U(\eta, t) = U(0, t) + \frac{\partial U}{\partial z} \eta . \quad (3.7)$$

Substitute (2.21) into (3.5) and use (3.7) and (3.3) which gives:

$$\frac{\partial A}{\partial z} (0, t) = -a[kc + \frac{dU}{dz}] , \quad (3.8)$$

$$\frac{\partial B}{\partial z} (0, t) = 0 \quad (3.9)$$



The condition  $U(0,t) \sim 0$  has been used. When (2.21) is substituted into (3.6), the following are obtained:

$$A(0,t) = ac , \quad (3.10)$$

$$B(0,t) = 0 . \quad (3.11)$$

The following boundary condition is used for the potential temperature fluctuation:

$$\theta(x,0,t) = 0 \quad (3.12)$$

This condition is not as accurate as the velocity conditions above, but the results shown later indicate that the temperature effects will be small in any case. Substituting (2.22) into (3.12) yields:

$$D(0,t) = E(0,t) = 0 \quad (3.13)$$

In order to close the problem, the following conditions are imposed at the top of the region:

$$A(H,t) = \frac{\partial A}{\partial z}(H,t) = B(H,t) = \frac{\partial B}{\partial z}(H,t) = D(H,t) = E(H,t) = 0 , \quad (3.14)$$

where  $z = H$  is the upper boundary.

The initial conditions are given by:

$$A(z,0) = ac \sinh[k(H_1 - z)] / \sinh kH_1 , \quad (3.15)$$

$$B(z,0) = 0 , \quad (3.16)$$

$$D(z,0) = 0 , \quad (3.17)$$

$$E(z,0) = 0 , \quad (3.18)$$

$$\text{and} \quad U(z,0) = \frac{U_*}{\kappa} \ln\left(\frac{z}{z_0} + 1\right) , \quad (3.19)$$





where:  $H_1 = H - \Delta z$ ,  $U_*$  = dynamic velocity,  $z_0$  = roughness parameter,  $\kappa = 0.35$  = von-Karman's constant, and  $a$  = wave amplitude. The equations give an irrotational initial state with no temperature fluctuations. The initial mean wind is logarithmic.

The following fields which are independent of time take the following form:

$$K = \kappa U_* z , \quad (3.20)$$

$$\tilde{\theta} = \frac{T_*}{\kappa} \ln \left( \frac{z}{z_0} + 1 \right) , \quad (3.21)$$

where  $T_*$  is the temperature scale.



#### IV. NUMERICAL PROCEDURES

Centered finite differences are introduced into equations (2.23) through (2.26) with the exception that the turbulence terms are evaluated at the previous time step. The left hand side of the equations are solved for the time tendencies with the Gauss elimination technique which is described in Richtmyer (1957). Centered time differencing is used except that the solution is restarted every 50 time steps with the finite difference scheme developed by Matsuno (1966). This procedure eliminates solution separation.

Note that the value of  $U$  given in equation (3.19) with the coefficient given by (3.20) leads to a zero value for the right hand side of (2.27). Therefore  $U$  can be expressed as follows:

$$U(z,t) = \frac{U^*}{K} \ln\left(\frac{z}{z_0} + 1\right) + \tilde{u}(z,t) . \quad (4.1)$$

Substitute (4.1) into (2.27) and integrate three times with respect to  $z$  which yields:

$$u = - \frac{1}{v} \int_0^z \tau \, dz , \quad (4.2)$$

$$\text{where } \tau = -uw = - \frac{1}{2}k \left( \frac{\partial B}{\partial z} A - \frac{\partial A}{\partial z} B \right) \quad (4.3)$$

is the Reynolds wave stress. In this derivation the right hand side of (2.27) was rewritten and the coefficient  $K$  was replaced by the constant  $v$ .



The boundary conditions (3.8), (3.9), (3.13), and (3.14) are applied in a straightforward manner with a one-sided derivative when required.

The time integration of the system of equations is accomplished by first solving the finite difference form of (2.23) through (2.26), and then computing the new  $U$  from equation (4.1). Integration is continued until a steady state is reached. The following quantity is used as a measure of the steadiness of the solution:

$$R = \left[ \sum_{i=1}^{i-\frac{H_1}{\Delta z}} [\tau(z_i, t) - \tau(z_i, t-\Delta t)]^2 \right]^{\frac{1}{2}} \quad (4.4)$$

The integration is continued until  $R_m \geq R$ , where  $R_m$  will take on three different values.



## V. NUMERICAL SOLUTIONS

The following constants were used in all numerical integrations:

$$\begin{aligned}U_* &= 0.167 \text{ m sec}^{-1} , \\z_o &= 7.9 \times 10^{-5} \text{ m} , \\v &= 0.24 \text{ m}^2 \text{ sec}^{-1} .\end{aligned}\tag{5.1}$$

Three forms of the boundary condition (3.8) were used in these numerical integrations. Stauffer (1973) used the following condition which neglects the  $\frac{\partial U}{\partial z}$  term:

$$\frac{\partial A}{\partial z}(0,t) = -akc .\tag{5.2}$$

The direct use of (3.19) in equation (3.8) leads to a singularity when applied at  $z = 0$ . In a private communication, Professor R. Davis has suggested that this problem can be alleviated by computing the derivative at a false level  $z = z_1$ . In this case the boundary condition becomes:

$$\frac{\partial A}{\partial z}(0,t) = -a[kc + \frac{U_*}{\kappa(z_1 + z_o)}] .\tag{5.3}$$

This formula reduces to (5.2) when  $z_1$  is very large. This procedure does not take into account changes in the mean wind near the surface through  $\tilde{u}$ .

A third boundary condition was used which changes as the mean wind changes. This takes the form:





$$\frac{\partial A}{\partial z}(0,t) = -a[kc + \frac{U(\Delta z,t) - U(0,t)}{\Delta z}] \quad (5.4)$$

Numerical solutions were obtained varying six independent parameters as shown in Table I. These were wave number ( $k$ ), wave amplitude ( $a$ ), measure of the error in the change of the stress in air ( $R_m$ ), false level ( $z_1$ ), temperature scale ( $T_*$ ), and the boundary condition  $\frac{\partial A}{\partial z}(0,t)$ . Experiments were carried out as exhibited in Table II for the different values shown in Table I.

Figures 1 and 2 show the distribution of mean wind velocity ( $U$ ) with height ( $z$ ) for series 1 and 2, respectively. These experiments use the lower boundary condition used by Stauffer (1973). Both figures show that the mean wind is close to the logarithmic profile for the largest wave numbers. They also show large variations as the wave number decreases. These departures are principally in the lower layers below approximately six meters. The smallest wave number ( $k = 0.050 \text{ m}^{-1}$ ) shows a much larger velocity than the logarithmic profile with a first maximum at approximately 1.5 meters. The character of the solutions for the two values of  $R_m$  are similar, but for particular wave numbers there are considerable differences.

Figures 3 and 4 represent series 3 for wave numbers  $k = 0.35 \text{ m}^{-1}$  and  $k = 0.20 \text{ m}^{-1}$ , respectively. These actually represent the Reynolds wave stress ( $\tau$ ) as a function of height. Curve six in each figure is for the case  $z_1 =$  infinity which corresponds to the boundary condition used



TABLE I. Values of the variables considered in the numerical experiments.

$k \text{ (m}^{-1}\text{)}$	$a \text{ (m)}$	$z_1 \text{ (m)}$	$R_m$	$\frac{\partial A}{\partial z}(0, t)$	$T_*$
0.050	0.10	0.025	$10^{-5}$	- akc	0.00
0.075					
0.100	0.25	0.075	$10^{-6}$	- a (kc + $\frac{U^*}{\kappa(z_1 + z_0)})$	0.15
0.125					
0.150	0.50	0.225	$10^{-7}$	- a (kc + $\frac{U(\Delta z, t) - U(0, t) - 0.15}{\Delta z}$ )	-0.15
0.175					
0.200	0.67	0.675			
0.225					
0.250	1.00	2.025			
0.275					
0.300	2.00	Infinity			
0.325					
0.350					
0.375					
0.400					
0.42535					
0.450					
0.475					
0.500					
1.000					



TABLE II. Experimental tests that were carried out using the values in Table I.

Series No.	Variable	$R_m$	$\frac{\partial A(0,t)}{\partial z}$	$T_*$	$\Delta z (m)$	$\Delta t (sec)$
1	Wave number (k)	$10^{-5}$	- akc	0.00	0.25	0.125
2	Wave number (k)	$10^{-6}$	- akc	0.00	0.25	0.125
* 3	False level ( $z_1$ )	$10^{-5}$	$- a(kc + \frac{U_*}{\kappa(z_1 + z_0)})$	0.00	0.25	0.125
4	Wave number (k)	$10^{-5}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.00	0.25	0.125
5	Wave number (k)	$10^{-6}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.00	0.25	0.125
6	Wave number (k)	$10^{-7}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.00	0.25	0.125
7	Wave number (k)	$10^{-5}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.00	0.125	0.003125
** 8	Wave amplitude (a)	$10^{-5}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.00	0.25	0.125
9	Wave number (k)	$10^{-5}$	$- a(kc + \frac{U(\Delta z, t) - U(0, t)}{\Delta z})$	0.15	0.25	0.125

\* carried out with wave number (k) =  $0.350 \text{ m}^{-1}$  and  $0.200 \text{ m}^{-1}$

\*\* carried out with wave number (k) =  $0.400 \text{ m}^{-1}$  and  $0.150 \text{ m}^{-1}$



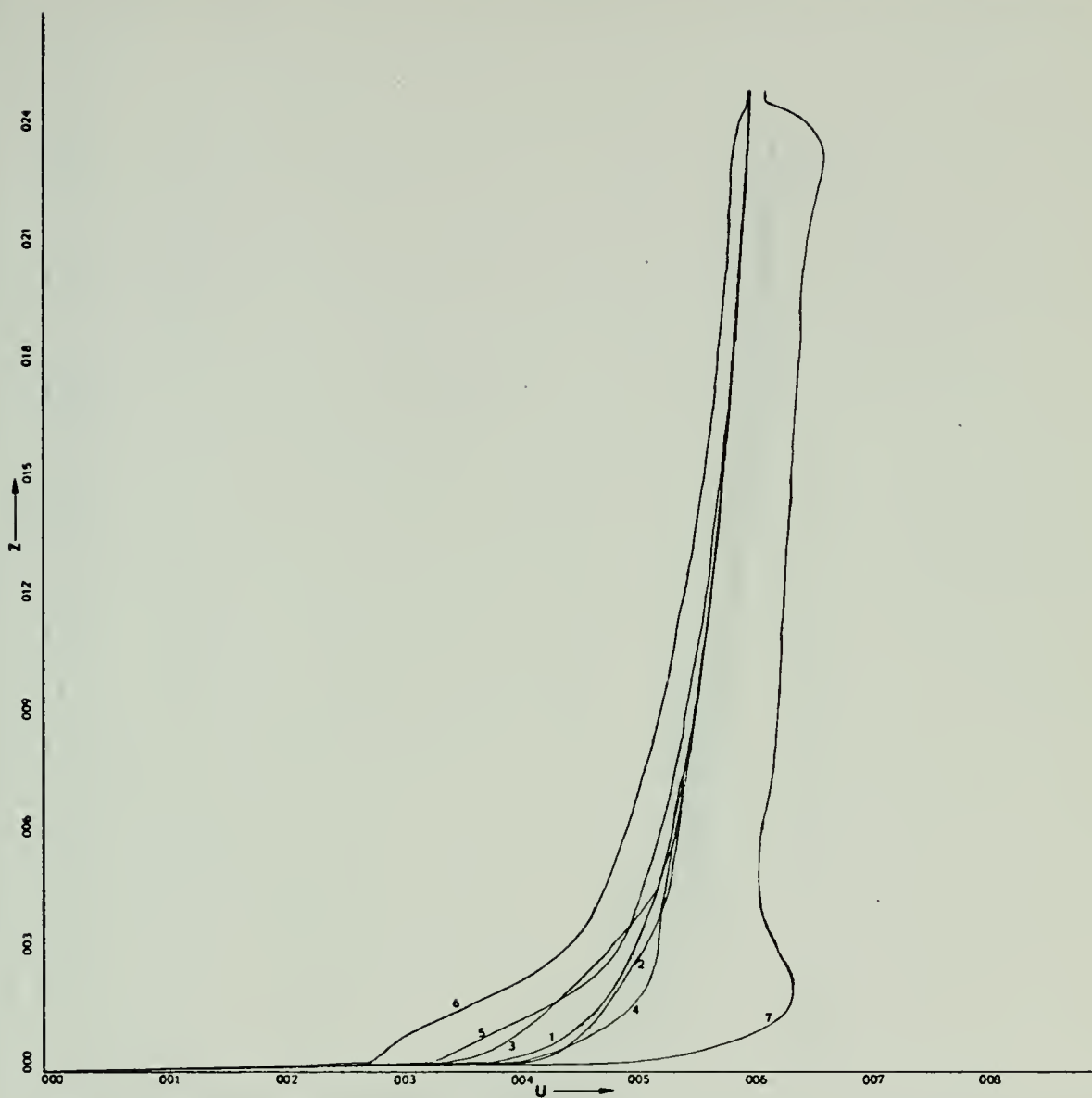


Figure 1. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 1 for wave number ( $k$ ) equal, respectively to: 1) initial mean velocity profile; 2)  $0.475 \text{ m}^{-1}$ ; 3)  $0.375 \text{ m}^{-1}$ ; 4)  $0.275 \text{ m}^{-1}$ ; 5)  $0.175 \text{ m}^{-1}$ ; 6)  $0.100 \text{ m}^{-1}$ ; 7)  $0.050 \text{ m}^{-1}$ .





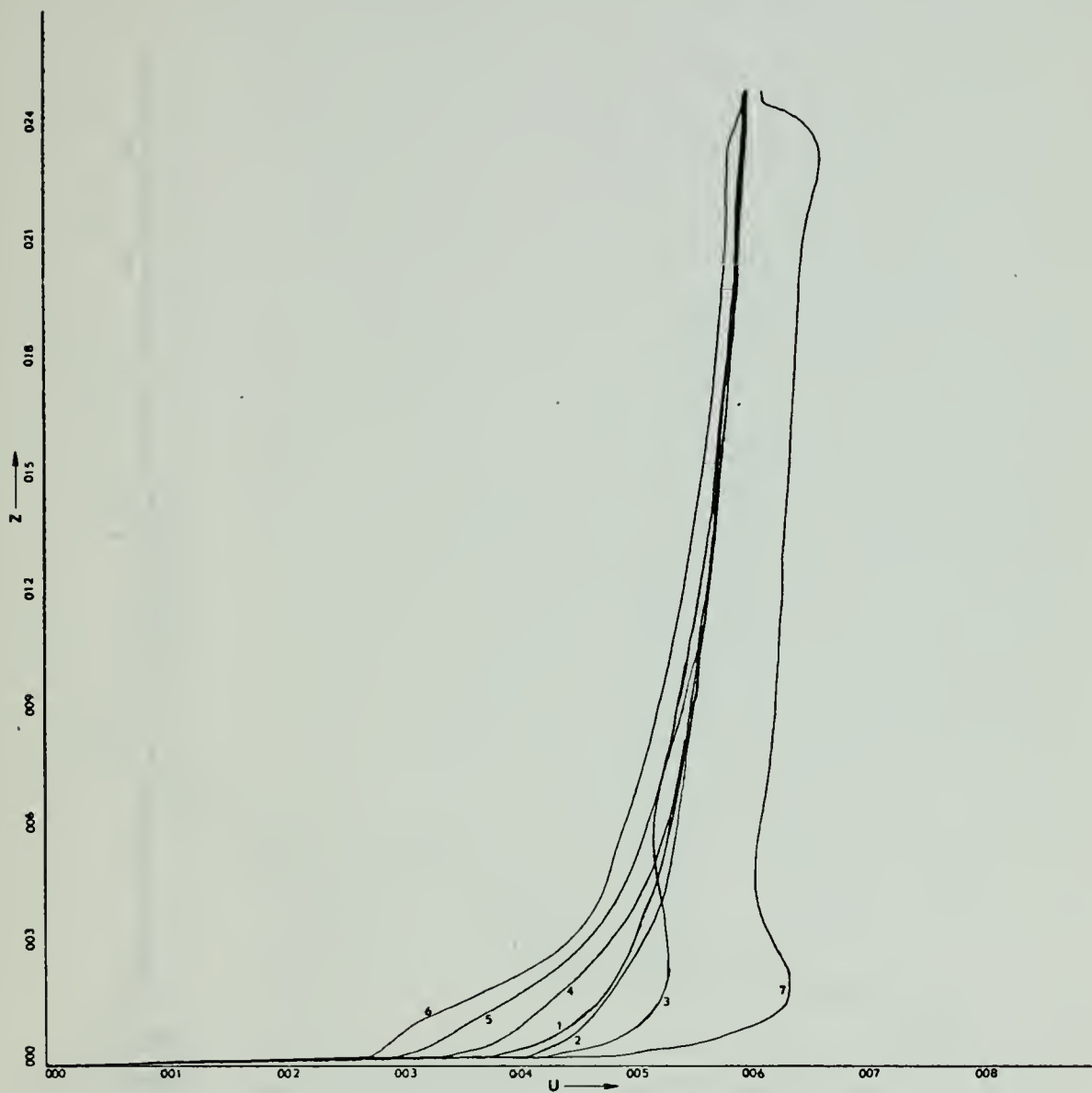


Figure 2. Distribution of mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 2 for wave number ( $k$ ) equal, respectively, to: 1) initial mean velocity profile; 2)  $0.475 \text{ m}^{-1}$ ; 3)  $0.375 \text{ m}^{-1}$ ; 4)  $0.275 \text{ m}^{-1}$ ; 5)  $0.175 \text{ m}^{-1}$ ; 6)  $0.100 \text{ m}^{-1}$ ; 7)  $0.050 \text{ m}^{-1}$ .



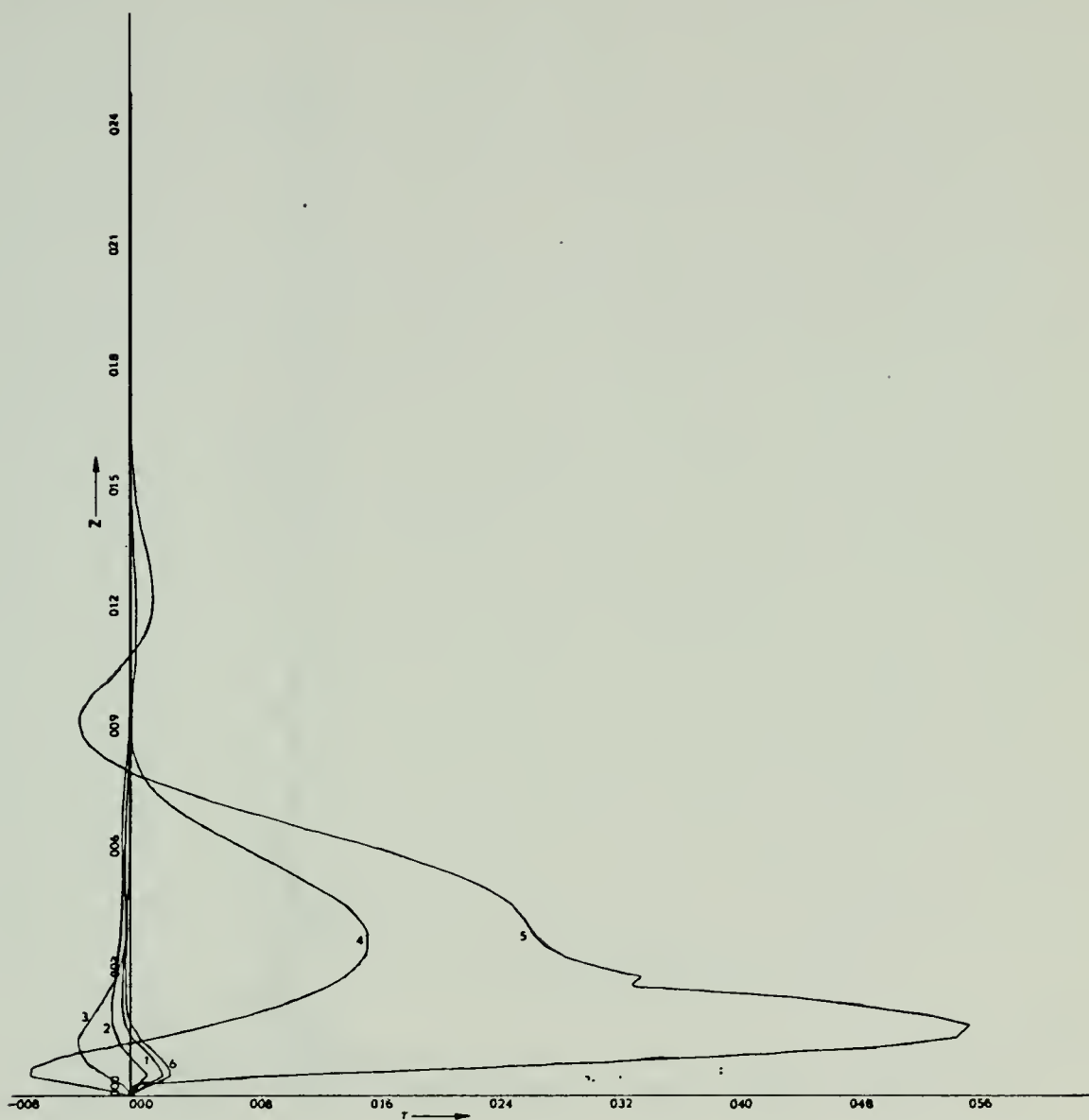


Figure 3. Distribution of the wave-caused stress ( $\tau$  in  $0.08 \text{ m}^2 \text{sec}^{-2}$ ) with height for wave number ( $k$ ) equal to  $0.350 \text{ m}^{-1}$ , and utilizing series 3. Variation in  $z_1$  is equal, respectively, to: 1) 2.025 m; 2) 0.675 m; 3) 0.225 m; 4) 0.075 m; 5) 0.025 m; 6) infinity.



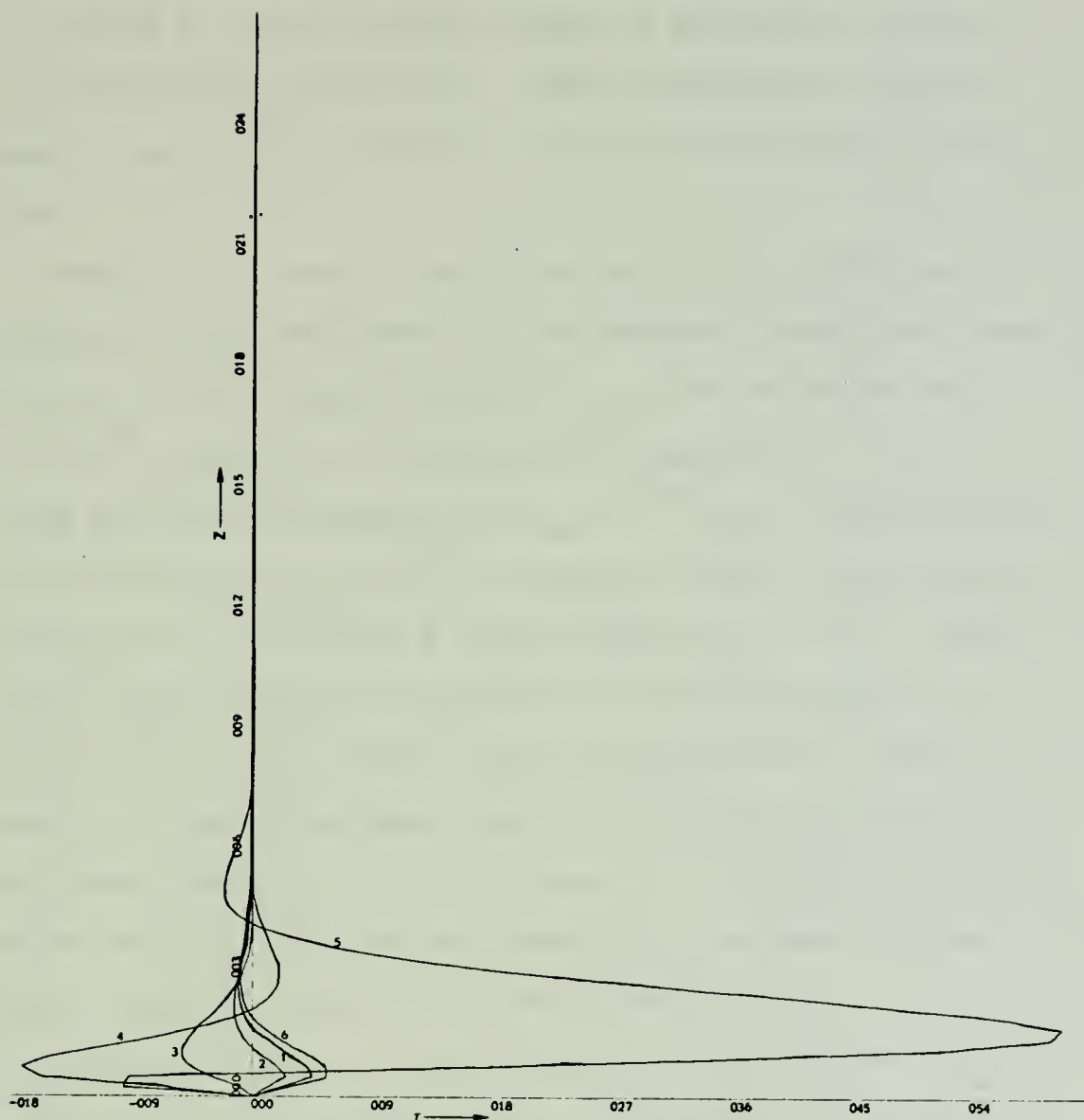


Figure 4. Distribution of the wave-caused stress ( $\tau$  in  $0.09 \text{ m}^2 \text{sec}^{-2}$ ) with height for wave number ( $k$ ) equal to  $0.200 \text{ m}^{-1}$ , and utilizing series 3. Variation in  $z_1$  is equal, respectively to: 1)  $2.025 \text{ m}$ ; 2)  $0.675 \text{ m}$ ; 3)  $0.225 \text{ m}$ ; 4)  $0.075 \text{ m}$ ; 5)  $0.025 \text{ m}$ ; 6) infinity.



by Stauffer (1973). These two curves are very similar to the curves for  $z_1 = 2.025$  m. As  $z_1$  decreases, the curve changes rapidly in such a way that the maximum stress for  $z_1 = 0.025$  m is at least one order of magnitude greater than the case  $z_1 = \text{infinity}$ . These experiments show the sensitivity of the solutions to this lower boundary condition.

Series 4, 5, and 6, which use the finite difference estimate of the wind shear in the boundary condition, were carried out with three values of  $R_m$ . The solutions for  $R_m = 10^{-5}$  and  $R_m = 10^{-6}$  showed some significant differences while the solutions for  $R_m = 10^{-7}$  were nearly identical for those of  $R_m = 10^{-6}$ . Figures 5 and 6 show the mean wind profile for series 5 which employs  $R_m = 10^{-6}$ . These figures show that for  $k \geq 0.450 \text{ m}^{-1}$  the wind profile is very close to the initial mean velocity profile. Also note the large departures from the logarithmic profile at low levels for  $k = 0.1 \text{ m}^{-1}$  or less. A disturbing feature of the solutions is the oscillation of the mean wind between adjacent values of the wave numbers.

Figure 7 shows the solutions for the mean wind for series seven. These solutions are the same as those of series 4 except that the grid size has been cut in half and the time step has been reduced to one-fourth. These solutions are generally similar to those in figures 5 and 6, except that in the lower levels the wind is larger than the logarithmic value for  $k \leq 0.42535 \text{ m}^{-1}$ . These results







Figure 5. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 5 for wave number ( $k$ ) equal, respectively, to: 1) initial mean velocity profile; 2)  $1.000 \text{ m}^{-1}$ ; 3)  $0.500 \text{ m}^{-1}$ ; 4)  $0.450 \text{ m}^{-1}$ ; 5)  $0.400 \text{ m}^{-1}$ ; 6)  $0.350 \text{ m}^{-1}$ ; 7)  $0.300 \text{ m}^{-1}$ .



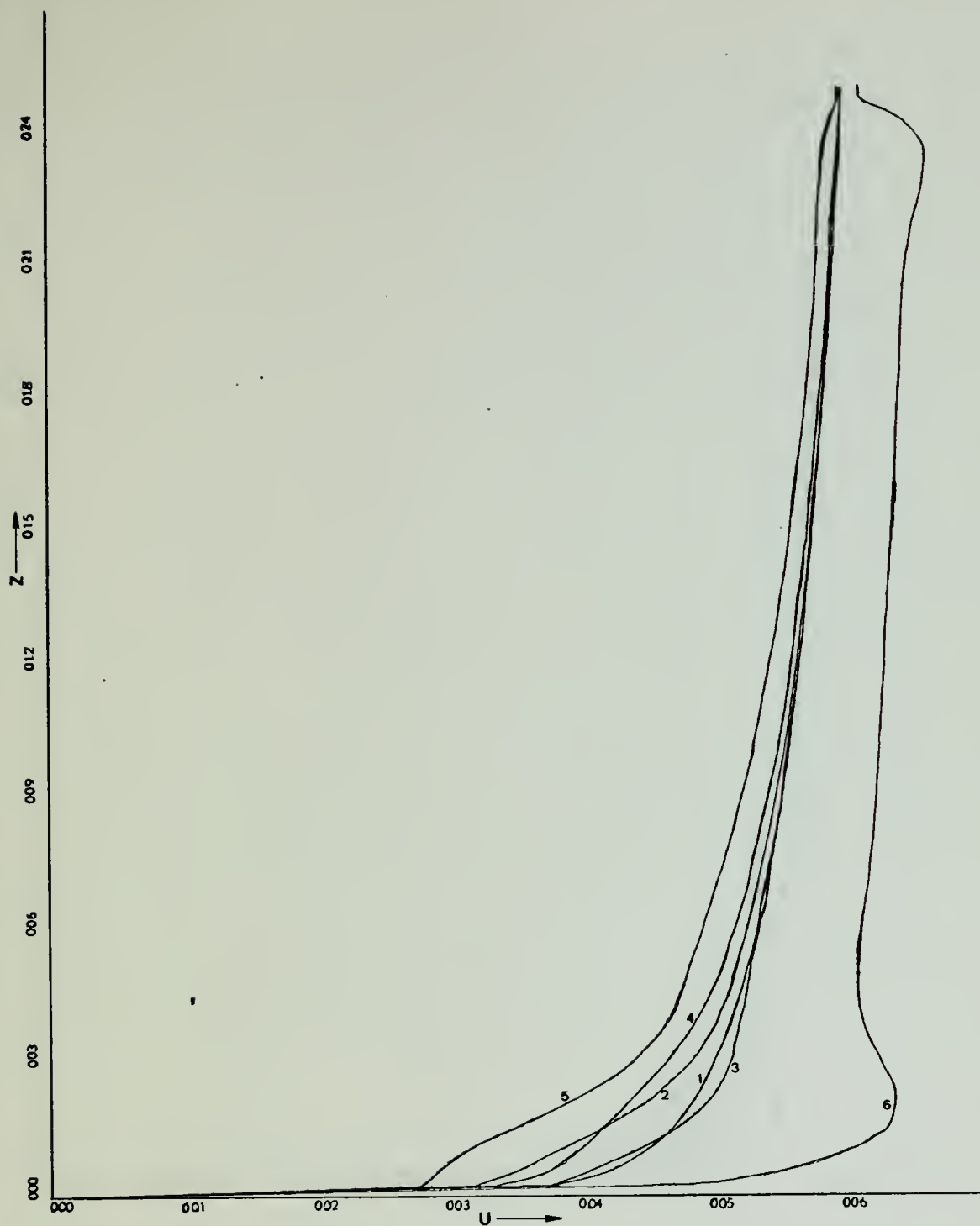


Figure 6. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 5 for wave number ( $k$ ) equal, respectively, to: 1) initial mean velocity profile; 2)  $0.250 \text{ m}^{-1}$ ; 3)  $0.200 \text{ m}^{-1}$ ; 4)  $0.150 \text{ m}^{-1}$ ; 5)  $0.100 \text{ m}^{-1}$ ; 6)  $0.050 \text{ m}^{-1}$ .



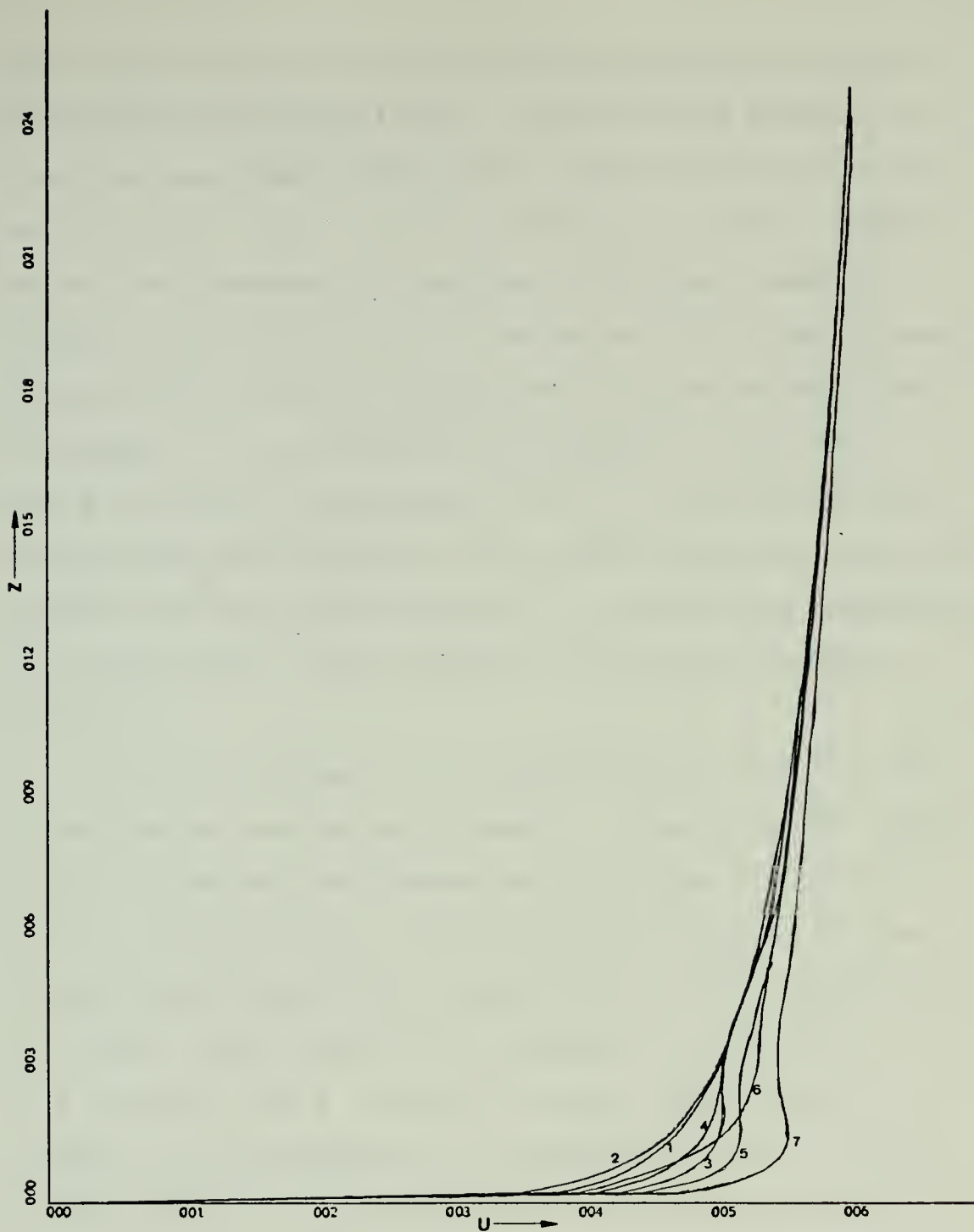


Figure 7. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 7 for wave number ( $k$ ) equal, respectively, to: 1) initial mean velocity profile; 2)  $1.000 \text{ m}^{-1}$ ; 3)  $0.42535 \text{ m}^{-1}$ ; 4)  $0.400 \text{ m}^{-1}$ ; 5)  $0.200 \text{ m}^{-1}$ ; 6)  $0.175 \text{ m}^{-1}$ ; 7)  $0.150 \text{ m}^{-1}$ .



are qualitatively consistent with the empirical relation developed by Davidson (1974). His data show departures from the logarithmic wind profile which are proportional to  $0.16 \left( \frac{C}{U_*} - 26.3 \right)$ . For this condition in these experiments, this quantity is positive for all wave numbers shown except for  $k = 1.0 \text{ m}^{-1}$  for which it is slightly negative. This behavior is consistent with the curves given in figure 7. One further test was made in this series for  $k = 0.200 \text{ m}^{-1}$  but with  $R_m = 10^{-6}$ . In that experiment the maximum wind velocity in the lower levels was very much larger than any shown in figure 7. This further emphasizes the sensitivity of the solutions to the lower boundary condition.

Figures 8 through 11 are comparisons of data already presented for certain wave numbers. Figure 8 shows identical solutions for the reduced grid size for  $k = 1.0 \text{ m}^{-1}$ . These solutions have a slightly smaller velocity in the lower layers than for the logarithmic profile. Figures 9, 10, and 11 which are for wave numbers  $k = 0.40 \text{ m}^{-1}$ ,  $k = 0.20 \text{ m}^{-1}$ , and  $k = 0.15 \text{ m}^{-1}$ , respectively, show irregular variations about the logarithmic profile for different values of  $R_m$ , but systematically higher values of wind speed for  $\Delta z = 0.125 \text{ m}$ .

Figures 12 and 13 contain the solutions from series 8 for wave numbers  $k = 0.40 \text{ m}^{-1}$  and  $k = 0.15 \text{ m}^{-1}$ , respectively. In all other experiments the wave amplitude is given by:





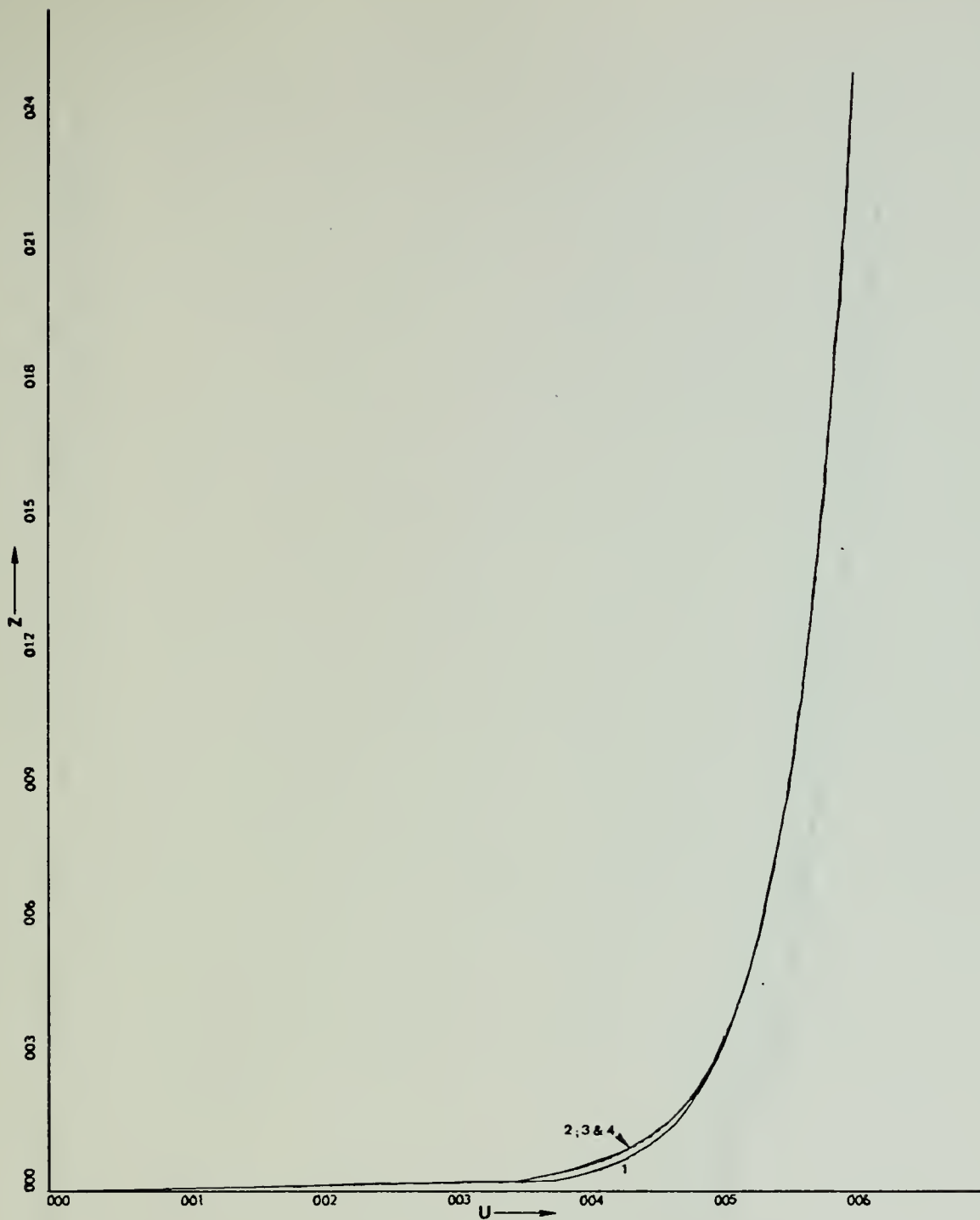


Figure 8. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) for wave number ( $k$ ) equal to  $1.000 \text{ m}^{-1}$ . Comparison is made where: 1) initial mean velocity profile; 2) series 4; 3) series 5 and 6; 4) series 7.





Figure 9. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) for wave number ( $k$ ) equal to  $0.0400 \text{ m}^{-1}$ . Comparison is made where: 1) initial mean velocity profile; 2) series 4; 3) series 5 and 6; 4) series 7.



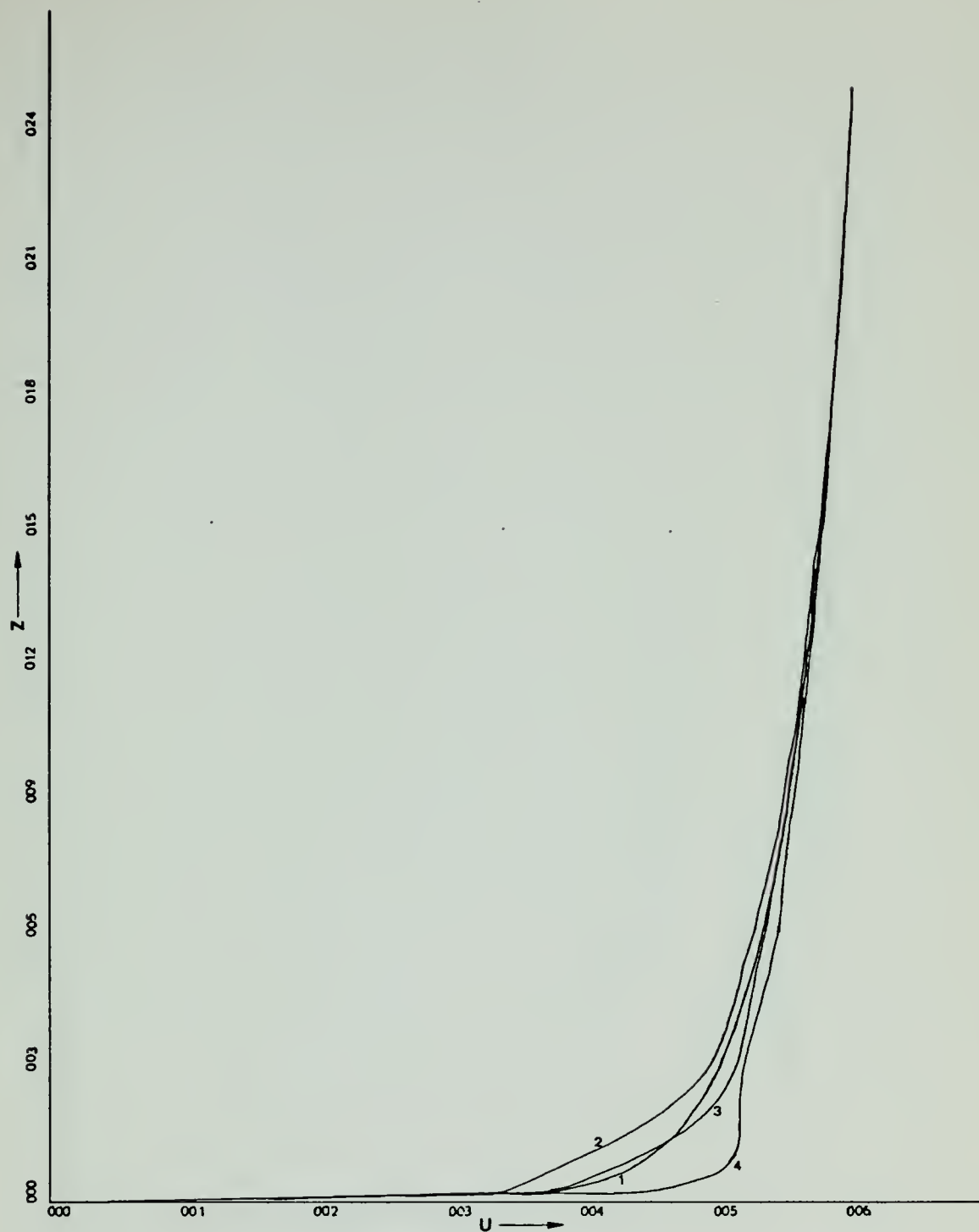


Figure 10. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) for wave number ( $k$ ) equal to  $0.200 \text{ m}^{-1}$ . Comparison is made where: 1) initial mean velocity profile; 2) series 4; 3) series 5 and 6; 4) series 7.



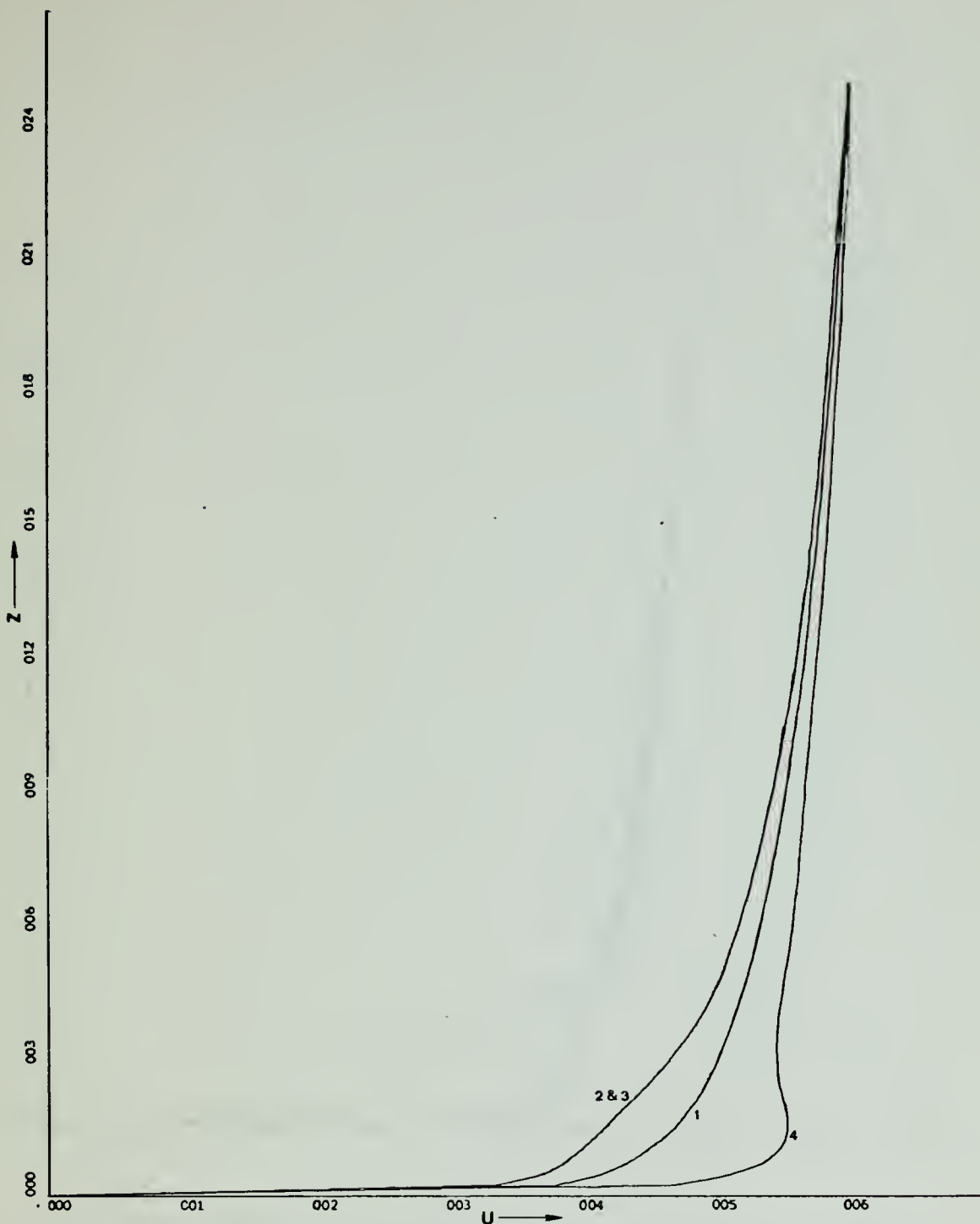


Figure 11. Distribution of mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) for wave number ( $k$ ) equal to  $0.150 \text{ m}^{-1}$ . Comparison is made where: 1) initial mean velocity profile; 2) series 4; 3) series 5 and 6; 4) series 7.





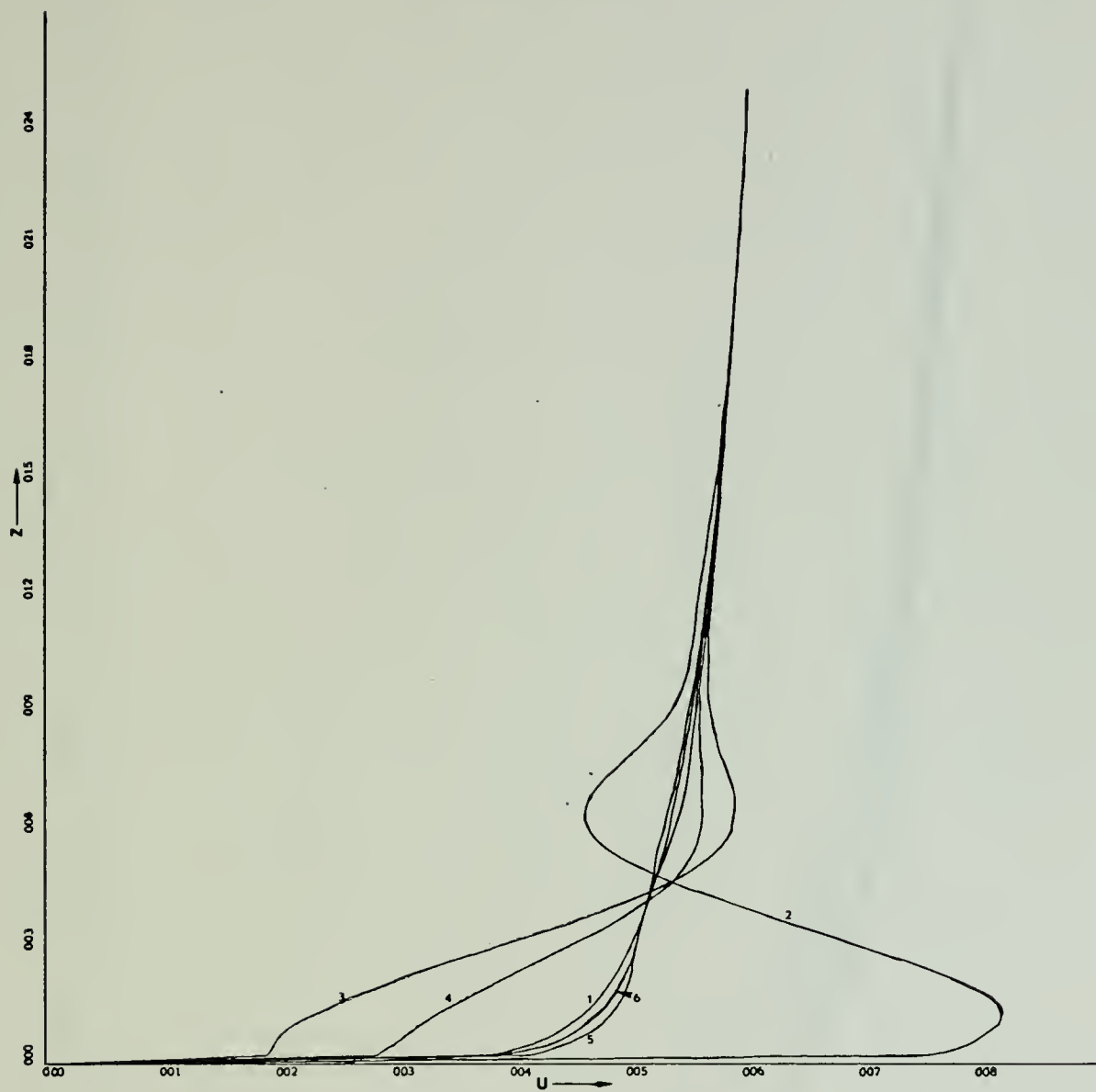


Figure 12. Distribution of the mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 8 for wave number ( $k$ ) equal to  $0.400 \text{ m}^{-1}$ . Variation in wave amplitude ( $a$  in meters) is equal, respectively, to: 1) initial mean velocity profile; 2) 2.00 m; 3) 1.00 m; 4) 0.50 m; 5) 0.25 m =  $.1/k$ ; 6) 0.10m.



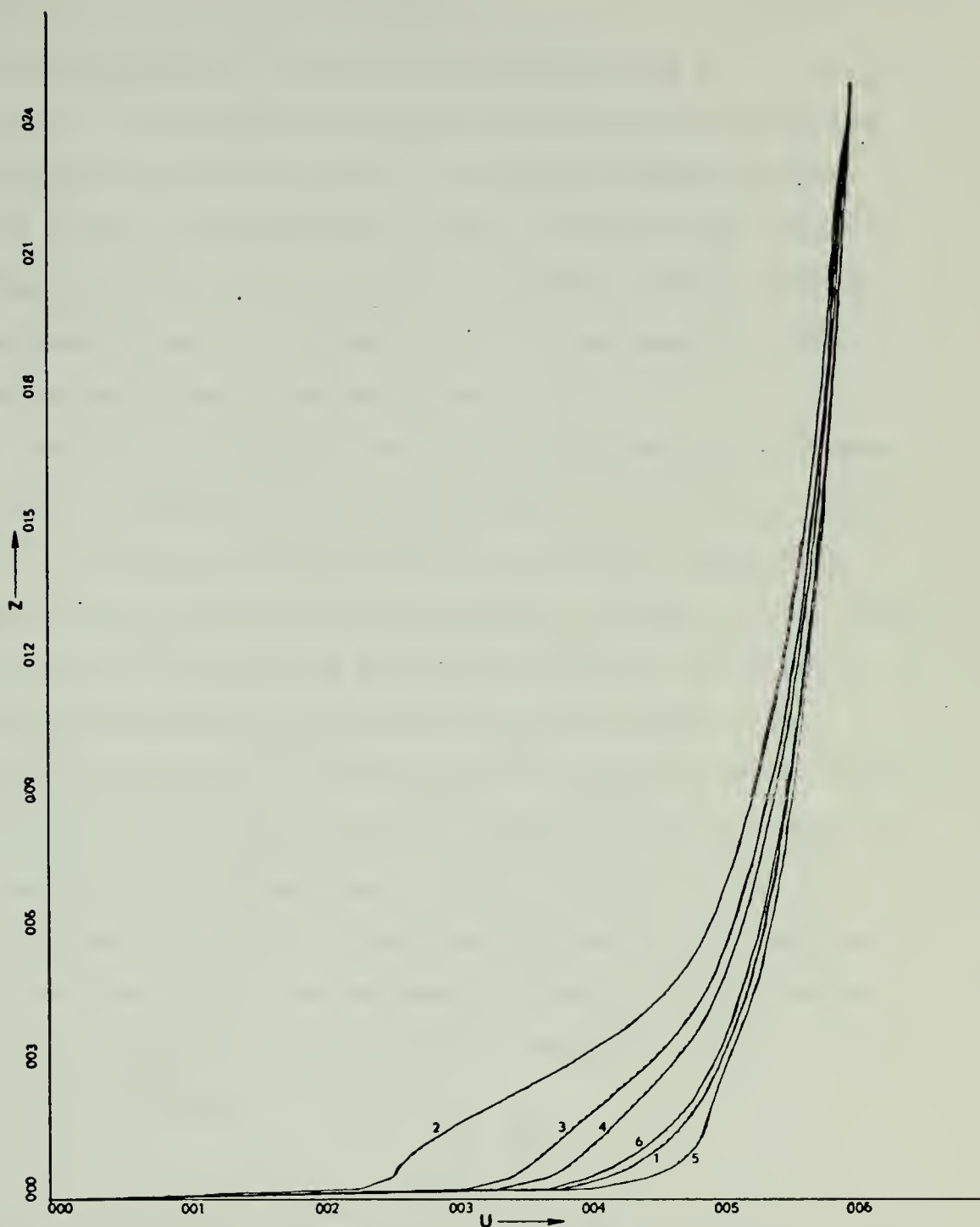


Figure 13. Distribution of mean wind velocity ( $U$  in  $\text{m sec}^{-1}$ ) with height ( $z$  in meters) utilizing series 8 for wave number ( $k$ ) equal to  $0.150 \text{ m}^{-1}$ . Variation in wave amplitude ( $a$  in meters) is equal, respectively, to:  
 1) initial mean velocity profile; 2) 2.00 m; 3) 1.00 m;  
 4)  $0.67 \text{ m} = .1/k$ ; 5) 0.50 m; 6) 0.10 m.



$$a = 0.1 k^{-1} \quad (5.5)$$

In these figures, the amplitude ranges from 0.10 m to 2.00 m. The smaller values of amplitude gives wind profiles which are very close to the logarithmic profile. The larger wave amplitudes lead to increasingly larger departures from the logarithmic profile. This is to be expected since  $\tilde{u}$  is proportional to the square of the disturbance amplitude (equation 4.2).

Figure 14 contains the disturbance potential temperature as a function of  $z$ , from series 9 with three values of  $k$ . These curves show that the largest temperature amplitudes occur at about one meter in height; above these maxima the temperature decreases rapidly. The largest amplitude occurs for the smallest wave number. The numerical solutions showed that the stream function amplitudes were not significantly affected by the presence of temperature fluctuations. This was true for both  $T_* = +0.15$  and  $T_* = -0.15$ . This behavior may be interpreted as follows. If it is assumed that the horizontal advection is balanced by the vertical advection, then equation (2.17) becomes:

$$\theta = \frac{1}{U-c} \frac{\partial \tilde{\theta}}{\partial z} \psi . \quad (5.6)$$

This expression is used to estimate the last term in (2.19). It can be seen that the buoyance term will be much smaller than the vorticity advection term with the possible



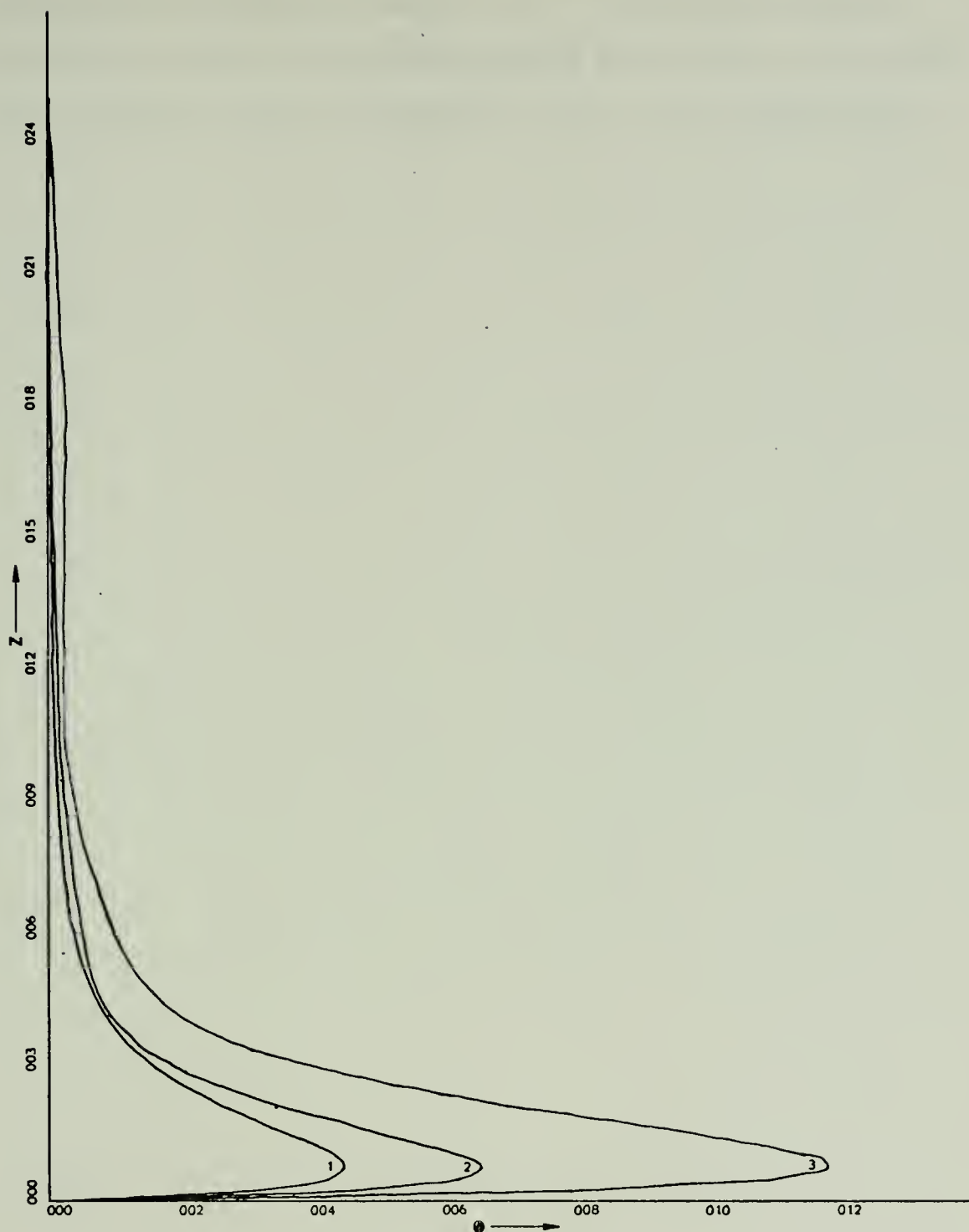


Figure 14. Distribution of disturbance potential temperature ( $\Theta$  in  $^{\circ}\text{K}$ ) with height ( $z$  in meters) utilizing series 9 for wave number ( $k$ ) equal, respectively, to: 1)  $0.275 \text{ m}^{-1}$ ; 2)  $0.125 \text{ m}^{-1}$ ; 3)  $0.050 \text{ m}^{-1}$ .





exception of the point where  $U = c$ . The numerical solutions show that the presence of such points does not change the conclusion that the buoyancy term is that unimportant.



## VI. CONCLUSIONS

In this study the numerical results of Stauffer (1973) were extended with the addition of buoyancy effects and two different lower boundary conditions. The buoyancy effects have no appreciable affect on the stream function and wind stress fields; however, the presence of buoyancy effects could affect the Reynolds wave stress through modifications in the mean wind profile. These effects were not considered in this study.

In this thesis, emphasis was placed on modifications in the mean profile which arose from the Reynolds wave stress. The two new boundary conditions which were investigated involved two methods of estimating  $\frac{\partial U}{\partial z}$  in one of the lower boundary conditions. This term was entirely neglected in the study by Stauffer (1973). In the first method the derivative was evaluated from the logarithmic wind profile evaluated at a false level ( $z_1$ ). This procedure leads to very large wave stresses near the surface when  $z_1$  became small.

In the second method,  $\frac{\partial U}{\partial z}$  was evaluated by finite differences. Many solutions were performed with this boundary condition involving different values of the wave number, convergence criteria, and the grid size. Those solutions showed that the wind profile was near the logarithmic profile for the larger wave numbers of order one.



Smaller wave numbers showed considerable fluctuation about the logarithmic profile in the lower layers with the tendency toward wind speeds larger than those given by the logarithmic profile. Figure 7, which employs the smallest grid size, shows this tendency clearly. However, further investigations with this profile suggest larger fluctuations if a finer convergence criteria is used. In general the computed wind profiles are consistent with observational data analyzed by Davidson (1974).

Further investigations of this type must carefully consider the lower boundary condition which was shown to be very sensitive in this study. Perhaps a full two-dimensional treatment of the air flow over the wave surface is required. Also it is very important to obtain accurate expressions for the turbulent exchange coefficients at different locations near the wave surfaces. These studies should be coordinated with careful analysis of observational data.



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wave numbers ( $k \geq 0.45\text{m}^{-1}$ ) or small wave amplitudes, 2) mean wind velocities at lower levels fluctuate more from the initial mean velocity profile as the wave number decreases or the wave amplitude increases, 3) solutions were very sensitive to the level where the velocity gradient is computed in the lower boundary condition, 4) disturbance potential temperature at lower levels increases inversely with wave number, and 5) the presence of temperature fluctuations has an insignificant effect on the Reynolds stress or on the stream function. The numerical solutions show general agreement with the observational analyses of wave modified wind profiles by Davidson (1974). However, these comparisons are not conclusive because of the sensitivity in the lower boundary condition.









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Numerical prediction of the mean wind ov



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